

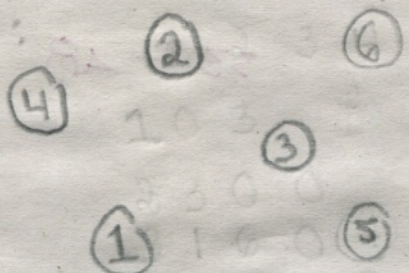
"TSO Midterm Exam"

Section ①

- ① ^{+4.5} it's an Optimization problem that have integer values but the decisions of the problem are boolean.
- ② ^{+4.5} To solve a C.O.P with brute-force method you need to solve the problem making all the possible ~~instances~~ ^{feasible solutions} and compare them to find the optimal solution.
- ③ ^{+2.5} it's an algorithm that try to solve a C.O.P in a rational amount of time.
- ④ ⁺⁴ it's preferable to use a heuristic method when the exact optimization method takes a lot of time to solve the problem.
- ⑤ ^{+3.5} it's a heuristic that use a greedy function to solve a problem. ^{how?}
- ⑥ ⁺⁷ To solve a T.S.P problem using the nearest neighbor heuristic we need to follow the next steps:
 - 1- Select a random city to start
 - 2- Go to the unvisited city closest to the last city picked
 - 3- Stop the process when the tour is completed, then calculate the total distance traveled.
 - 4- Repeat the process until you find the best tour (the one with the lowest total distance traveled).

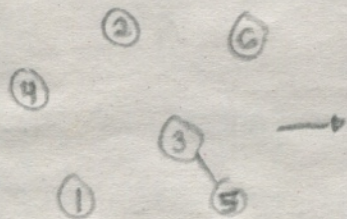
Example: We picked randomly the city number 3

Solve:

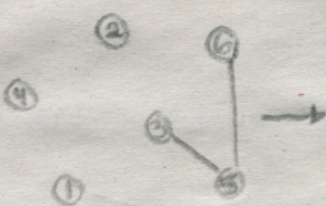


* Note: This is an example of a feasible solution.

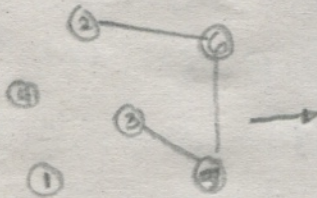
Iteration 1:



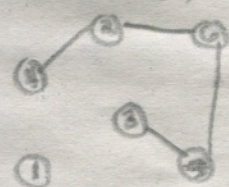
Iteration 2:



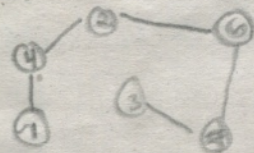
Iteration 3:



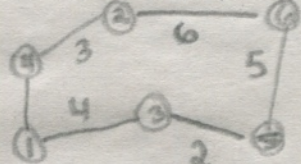
Iteration 4:



Iteration 5:



Iteration 6:



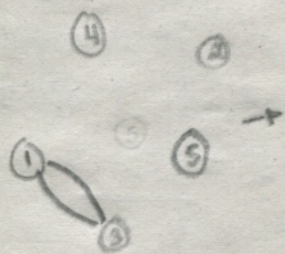
$$\text{distance traveled} = 2 + 5 + 6 + 3 + 4 = \underline{20}$$

7 To solve a T.S.P with the nearest insertion heuristic we need to follow the next steps:

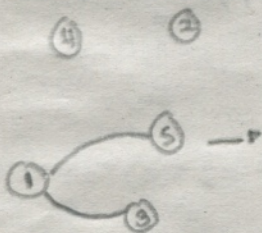
- 1- Choose a starting node and add it to the solution.
- 2- Find the closest node to the starting node and add it to the solution.
- 3- For each subsequent node to be added to the solution, find the pair of nodes in the current solution that are the closest to it.
- 4- Select the pair of nodes that minimized the distance when the new node is inserted. (Formula: $C_{ik} + C_{jk} - C_{ij}$)
- 5- Insert the between the selected pair of nodes.
- 6- Repeat Step 3 to 5 until we add all the nodes.
- 7- Connect the last node with the initial node to get a tour and completed the solution.

Example: We started with the node ①

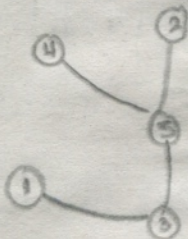
Iteration 1:



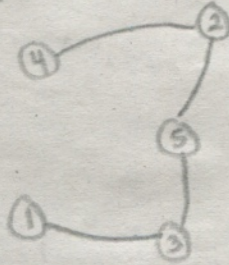
Iteration 2:



Iteration 3:

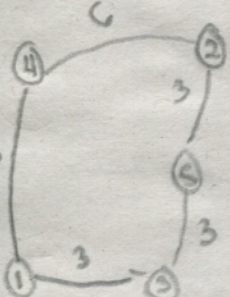


Iteration 4:



Iteration 5:

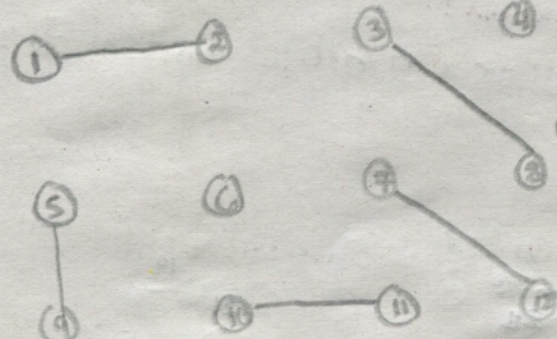
Total distance traveled = $3 + 3 + 3 + 6 + 6 = 21$



⑧

a)

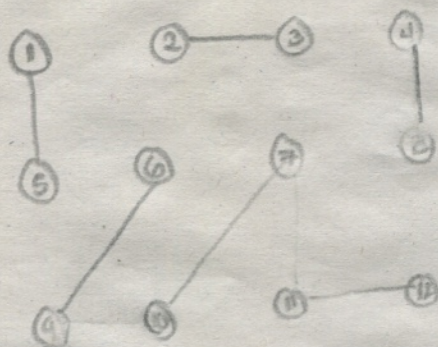
14



A= Yes, it is a feasible solution because met the constrain which is that there are not two or more edges sharing the same node.

But it's not perfect

b)



A = Yes, it's a feasible solution because it met the constrain which is that there are not two or more edges sharing the same node.

+ A (6,4) does not exist

c) + 5

$M^3 = \{(1,5), (2,6), (3,7), (4,8), (7,11), (9,10)\}$ = This solution it's not feasible, because it doesn't met the constrain, (node 7)

$$M^4 = \{(1,2), (5,9), (6,10), (3,7), (4,8), (11,12)\} = 17 + 30 + 19 + 16 + 15 + 18 = 115$$

$$M^5 = \{(1,5), (2,6), (9,10), (3,4), (7,11), (8,12)\} = 14 + 14 + 18 + 19 + 14 + 26 = 105$$

A = 1 = M^4 , 2 = M^5 BEST
 M^3 = it's not a feasible solution so it's the WORST

d) To solve the MP problem using the most value edge we need to follow the next steps:

1 = Find the most value edge available of the problem.

2 = Verify that there's not a vertex connected to the node.

3 = Put a vertex which? Why? Explain?

4 = Repeat step 1 to 3 until you put the max available vertex to put

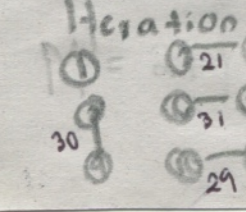
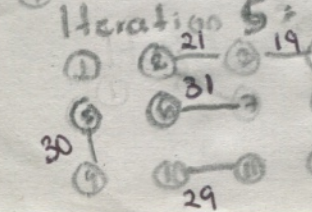
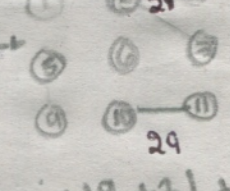
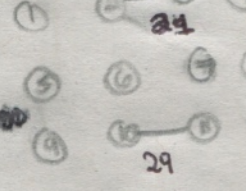
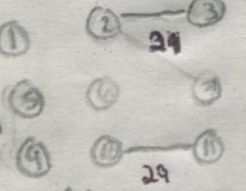
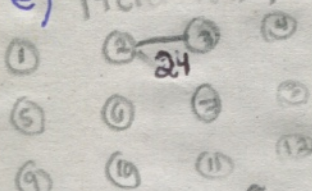
5 = Calculate M.

e) Iteration 1:

Iteration 2:

Iteration 3:

Iteration 4:



$$M = 21 + 29 + 26 + 19 + 31 + 30 = 156$$

$$50 \quad 76 \quad 95 \quad 124$$